



**NATIONAL UNIVERSITY OF ENGINEERING**  
**COLLEGE OF GEOLOGICAL, MINING AND METALLURGICAL**  
**ENGINEERING**

**METALLURGICAL ENGINEERING PROGRAM**

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**MA311 – STATISTICS AND PROBABILITIES**

**I. GENERAL INFORMATION**

<b>CODE</b>	: MA311 Statistics and Probabilities
<b>SEMESTER</b>	: 3
<b>CREDITS</b>	: 4
<b>HOURS PER WEEK</b>	: 6 (Theory – Practice – Labs)
<b>PREREQUISITES</b>	: MA123 Mathematics II
<b>CONDITION</b>	: Compulsory

**II. COURSE DESCRIPTION**

This course prepares students in the application of concepts, methods and techniques of the differential and descriptive statistics to describe and analyze data and variable sets. Concepts of probability and random variables are introduced and applied to predict expected future values. Regression techniques are applied to build models relating a data and variable set. Problems of engineering application are solved and specialized software is used too.

**III. COURSE OUTCOMES**

1. Organize data for their adequate analysis and interpretation and calculate and interpret their fundamental statistical properties (Average value y variance).
2. Explain and determine the random probability of events and variables, as well as their probability density function.
3. Understand and apply random vectors and determine their function of joint probability density.
4. Interpret the concept of sampling distribution and apply it to calculate the probability of an event or variable.
5. Build models of linear regression to represent the relationship between the representative parameters of a data set.
6. Apply chi-square tests to check the probability density function of a data set, as well as the dependence or independence of two variables.

**IV. LEARNING UNITS**

**1. DATA ORGANIZATION AND MAIN STATISTICAL PARAMETERS / 8 HOURS**

Statistics / Population, sample and variable / Classification of variables / Methods for organizing and presenting data / Qualitative data / Frequency distribution table / Graphic representations / Measures of central tendency: mean, median, weighted mean / Dispersion methods: variance, standard deviation, coefficient of variation / Measures of quartile, decile and percentile positions / Box plots.

**2. PROBABILITY / 8 HOURS**

Count methods / Addition and multiplication rules / Permutations and combinations / Probability / Random experiments, sampling space and events / Operations with events / Conditional probability / Total probability / Bayes' theorem / Tree chart / Independent events.

**3. RANDON VARIABLES AND PROBABILITY DISTRIBUTION / 12 HOURS**

Random variable: Types, expected value and standard deviation / Distribution of probability of a discrete variable: binomial, Poisson and hyper-geometric / Distribution of probability of a continuous variable: uniform, normal, gamma and exponential.

#### **4. RANDOM VECTORS / 4 HOURS**

Joint probability density function / Marginal distribution / Expected vector, variance and covariance / expected value of two random functions / Covariance of two random variables.

#### **5. SAMPLING DISTRIBUTION / 4 HOURS**

Sampling / Sampling techniques / Probability sampling / Sampling distribution of average value, the variance / Central limit theorem.

#### **6. ESTIMATION AND HYPOTHESIS TESTING / 12 HOURS**

Punctual estimation of a random sampling / Punctual estimators: mean, mean proportional, difference of means, variance / Hypothesis testing / Interval estimation. Confidence intervals: mean, mean proportional and variance / Hypothesis testing / Types of error / Correlation coefficient / Prediction intervals / Hypothesis testing on regression coefficients.

#### **7. REGRESSION AND CORRELATION ANALYSIS / 8 HOURS**

Simple regression / Scatter plot / Parameter estimation / Total variance decomposition / Determination coefficient / Estimation errors / Correlation coefficient / prediction intervals / Hypothesis testing on regression coefficients.

#### **8. CHI-SQUARE TESTS / 8 HOURS**

Setting tests for uniform, binomial and Poisson's distributions / Contingency tables / Independence tests.

### **V. LABORATORIES AND PRACTICAL EXPERIENCES**

Lab 1: Generation of random signals.

Lab 2: Determination and graphs of the probability density function.

Lab 3: Linear and quadratic regression.

### **VI. METHODOLOGY**

This course is carried out in theory, practical and lab sessions. In theory sessions, the instructor introduces concepts, theorems and applications. In practical sessions, several problems are solved and their solution is analyzed. In lab sessions, Minitab simulation software is used to solve problems and analyze their solutions. At the end of the course, students should hand in and expose an integrating paper and project. In all sessions, students' active participation is encouraged.

### **VII. EVALUATION FORMULA**

The average grade PF is calculated as follows:

$$PF = 0.25 EP + 0.25 EF + 0.10 P1 + 0.10 P2 + 0.07 L1 + 0.07 L2 + 0.07 L3 + 0.09 TF$$

EP: Mid-Term Exam

EF: Final Exam

TF: Final paper

P: Quizzes

L: Final paper

### **VIII. BIBLIOGRAPHY**

1. **MENDENHALL, WILLIAM**  
Statistics and probability for engineering (Spanish)  
Prentice Hall Editorial (2005)
2. **ALVAREZ, JOSÉ AND TORRES LUIS**  
Probability and Statistics (Spanish)  
Alfa Omega Editorial (2006)
3. **MONTGOMERY, DOUGLAS AND RUNGER GEORGE**  
Probability and Statistics Applied to Engineering (Spanish)  
McGraw Hill Editorial (2008)

## IX. COURSE CONTRIBUTIONS TO STUDENT OUTCOMES ATTAINMENT

Course contributions to Student Outcomes are shown in the following table:

Level 1: Know

Level 2: Comprehend, calculate

Level 3: Model, apply, solve

Level 4: Apply at advanced level, design. Achievement of Student Outcome

Outcome	Contribution
<b>1. Engineering Design</b> Design and integrate metallurgical systems and components satisfying requirements and needs as well as given technical, economic, social and legal constraints and limitations.	
<b>2. Problem solving</b> Identify, formulate and solve engineering problems properly using the methods, techniques and tools of metallurgical engineering.	2
<b>3. Sciences Application</b> Apply the knowledge and skills of mathematics, sciences and engineering to solve metallurgical engineering problems.	2
<b>4. Experimentation and Testing</b> Conceive and conduct experiments and tests, analyze data and interpret results.	2
<b>5. Modern Engineering Practice</b> Use and apply techniques, methods and tools of modern engineering necessary for the practice of metallurgical engineering.	2
<b>6. Engineering Impact</b> Understand the impact of metallurgical engineering solutions on people and society in local and global contexts.	2
<b>7. Project Management</b> Determine the budgets, schedules and feasibility of engineering projects, and participate in its management for the attainment of goals.	
<b>8. Environmental Appraisal</b> Take into account the importance of preserving and improving the environment in the development of their personal and professional activities.	2
<b>9. Lifelong Learning</b> Recognize the need to keep their knowledge and skills up-to-date according to advances of metallurgical engineering and engage in lifelong learning.	2
<b>10. Contemporary Issues</b> Know and analyze relevant contemporary issues in local, national and global contexts.	2
<b>11. Ethics and Professional Responsibility</b> Evaluate their decisions and actions from a moral perspective and assume responsibility for the executed projects.	
<b>12. Communication</b> Communicate clearly and effectively in oral, written and graphical formats, interacting with different types of audiences.	2
<b>13. Teamworking</b> Appraise the importance of teamworking and participate actively and effectively in multidisciplinary teams.	2